

## Funções

Domain → Codomain

One to One (Interjections)	Functions that assign every domain value to a different codomain value.
Onto (Surjections)	Every codomain value has at least one domain value assigned to it.
Bijections	A function that's both an interjection and a surjection.

## Números Primos

2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47, 53, 59, 61, 67, 71, 73, 79, 83, 89, 97

Least Common Multiple: The smallest integer divisible by both a and b when  $\text{lcm}(a, b)$ .

Greatest Common Divisor: The greatest positive common divisors between two numbers when  $\text{gcm}(a, b)$ .

Numbers are relatively prime if their greatest common divisor is 1.

## Formulários de Somação

Sum	Closed Form	Sum	Closed Form
$\sum_{k=0}^n ar^k (r \neq 0)$	$\frac{ar^{n+1} - a}{r-1}, r \neq 1$	$\sum_{k=1}^n k^3$	$\frac{n^2(n+1)^2}{4}$
$\sum_{k=1}^n k$	$\frac{n(n+1)}{2}$	$\sum_{k=0}^{\infty} x^k,  x  < 1$	$\frac{1}{1-x}$
$\sum_{k=1}^n k^2$	$\frac{n(n+1)(2n+1)}{6}$	$\sum_{k=1}^{\infty} kx^{k-1},  x  < 1$	$\frac{1}{(1-x)^2}$

## O Algoritmo Euclidiano

$\text{gcd}(a, b)$  — find the last non zero remainder using long division  $\frac{a}{b}, \frac{b}{R}$ .

## Congruencia

$x \equiv y \pmod{z}$  if  $(x - y) \mod z = 0$

$$ax \equiv b \pmod{c} \rightarrow x \equiv n \pmod{c} \leftarrow an + cm = b \leftarrow b = aw_1 + r_1$$

$$a = r_1 w_2 + r_2$$

## 中國剩餘定理

System of $n$ Equations	$r_i$	$M_i$ when $M = \sum_{i=1}^n m_i$	$x_i \Leftarrow M_i x_i \equiv 1 \pmod{m_i}$
$x \equiv a \pmod{m_1}$	$a$	$\frac{M}{M_1}$	$M_1 x_i \equiv 1 \pmod{m_1}$
$x \equiv b \pmod{m_2}$	$b$	...	...
$x \equiv c \pmod{m_3}$	$c$	...	...

$$s = \sum_{i=1}^n x_i \Rightarrow x = s \mod M$$